

MATH 158 Assignment 5, Spring 2010

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Due Tuesday April 6th at 5:20 pm.

Dear class, I'd like to remind you that you need to do the assignment exercises to understand the material. If you do this you will be well prepared for the final exam. Mike M.

14.1 Taylor Polynomials

Exercises 17, 18, 24, 33, 34, 48.

14.2 Infinite Sequences

Exercises 2, 5, 34, 36, 40, 49, 50.

14.3 Infinite Series

Exercises 2, 10, 12, 35, 36, 48.

14.4 Series with Positive Terms

Exercises 4, 8, 11, 12, 13, 33, 34, 52.

11.3 Applications of Differential Equations

11.3 Exercises 7 and 12 plus the following bonus exercise.

Exercise 17 of 11.3 used $P'(t) = kP(t) + I$ to model population growth of a country with constant (net) migration I . Here $P(t)$ is the population at time t and k is the natural growth rate. In exercise 18, using data for Canada from 1990, you solved the DE for $P(0) = 22$ million, $k = 0.8\%$ per year, and $I = 0.2$ million per year. But $k = 0.8\%$ is not accurate for 2010. Using google, I found out that currently, each woman in Canada has on average 1.50 babies in her lifetime (this has remained almost constant over the last 10 years) and that the average age of a woman giving birth is now 29.6 years (this has been increasing slowly). This means that the population under 50 years of age is now in decline; in 29.6 years, the population under 50, in the absence of migration, will shrink by 25%. Using this data show that the natural growth rate for Canada is now $k = -0.00972$.

Given the current population of Canada is 34.0 million and current net migration is $I = 0.2$ million per year, using $k = -0.00972$, solve $P'(t) = kP(t) + I$ for $P(t)$. If k and I do not change, what would the long term population in Canada be? [Hint: take $\lim_{t \rightarrow \infty} P(t)$] If k does not change, what net migration rate I is needed to offset the natural decline in the population? [Hint: if $P(0) = 34$ million, and $k = -0.00972$, what value of I is needed so that $P'(t) = 0$?