

Modular Multiplication algorithm.

**> A := x^4+25\*x^3+145\*x^2-171\*x-360;**

$$A := x^4 + 25x^3 + 145x^2 - 171x - 360 \quad (1)$$

**> B := x^5+14\*x^4+15\*x^3-x^2-14\*x-15;**

$$B := x^5 + 14x^4 + 15x^3 - x^2 - 14x - 15 \quad (2)$$

**> Bound := maxnorm(A)\*maxnorm(B)\*min(nops(A),nops(B));**

$$\text{Bound} := 27000 \quad (3)$$

**> p1 := 43;**

**modp(A,p1);**

**C1 := modp( expand(modp(A,p1) \* modp(B,p1)), p1 );**

$$\begin{aligned} p1 &:= 43 \\ C1 &:= x^9 + 39x^8 + 37x^7 + 40x^6 + 27x^5 + 12x^4 + 20x^3 + 20x^2 + 37x + 25 \end{aligned} \quad (4)$$

**> p2 := nextprime(p1);**

**C2 := Expand(A\*B) mod p2;**

$$\begin{aligned} p2 &:= 47 \\ C2 &:= x^9 + 39x^8 + 40x^7 + 24x^6 + 40x^5 + 16x^4 + 27x^3 + 15x^2 + 38x + 42 \end{aligned} \quad (5)$$

**> p3 := nextprime(p2);**

**C3 := Expand(A\*B) mod p3;**

$$\begin{aligned} p3 &:= 53 \\ C3 &:= x^9 + 39x^8 + 33x^7 + 7x^6 + 18x^5 + 47x^4 + 51x^3 + 49x^2 + 26x + 47 \end{aligned} \quad (6)$$

**> M := p1\*p2\*p3;**

$$M := 107113 \quad (7)$$

**> C := chrem( [C1,C2,C3], [p1,p2,p3] );**

$$C := x^9 + 39x^8 + 510x^7 + 2233x^6 + 106495x^5 + 98998x^4 + 99479x^3 + 579x^2 + 7605x + 5400 \quad (8)$$

Put G in the symmetric range for the integers modulo m.

**> mods( C, M );**

$$x^9 + 39x^8 + 510x^7 + 2233x^6 - 618x^5 - 8115x^4 - 7634x^3 + 579x^2 + 7605x + 5400 \quad (9)$$

**> expand( A\*B );**

$$x^9 + 39x^8 + 510x^7 + 2233x^6 - 618x^5 - 8115x^4 - 7634x^3 + 579x^2 + 7605x + 5400 \quad (10)$$